

1. Objective

- Introduction to SAS PROC MIXED
- Analyzing protein milk data using STATA
- Refit protein milk data using PROC MIXED

2. Introduction to SAS PROC MIXED

The MIXED procedure provides you with flexibility of modeling not only the means of yours data (as in the standard linear model) but also their variances and covariance as well (the mixed linear model).

- **THE MIXED LINEAR MODEL**

- **The standardized linear model**
 - $\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\epsilon}$
 - $\boldsymbol{\beta}$ is an unknown vector of fixed-effects parameters with known design matrix \mathbf{X} .
 - $\boldsymbol{\epsilon}$ is assumed to be independent and identically distributed Gaussian random variables with mean 0 and variance σ^2 .
 - **The mixed linear model**
 - a generalized version of the standardized linear model as follows:
$$\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{Z}\boldsymbol{\gamma} + \boldsymbol{\epsilon}$$
 - $\boldsymbol{\gamma}$ is an unknown vector of random-effects parameters with known design matrix \mathbf{Z}
 - $\boldsymbol{\epsilon}$ is the residuals vector whose elements are no longer required to be independent and homogeneous, and its variance is \mathbf{R} .
 - The variance of \mathbf{Y} is $\mathbf{V} = \mathbf{ZGZ}' + \mathbf{R}$
 - For G and R, you must select some covariance structure.

- **SYNTAX: (details refer to SAS help)**

```
PROC MIXED < options > ;  
BY variables ;  
CLASS variables ;  
ID variables ;  
MODEL dependent = < fixed-effects > < / options > ;  
RANDOM random-effects < / options > ;  
REPEATED < repeated-effect > < / options > ;  
PARMS (value-list) ... < / options > ;  
PRIOR < distribution > < / options > ;  
CONTRAST 'label' < fixed-effect values ... >  
< | random-effect values ... >, ... < / options > ;  
ESTIMATE 'label' < fixed-effect values ... >  
< | random-effect values ... >< / options > ;  
LSMEANS fixed-effects < / options > ;  
MAKE 'table' OUT=SAS-data-set ;  
WEIGHT variable ;  
RUN;
```

Let's look at **method=options** for **PROC, CLASS, MODEL, RANDOM, and REPEATED**.

- **Method=option**

The METHOD= option specifies the estimation method for the covariance parameters. The REML specification performs restricted maximum likelihood, and it is the default method. The ML specification performs maximum likelihood.

- **CLASS**

- The CLASS statement names the classification variables to be used in the analysis.
- If the CLASS statement is used, it must appear before the MODEL statement.
- Classification variables can be either character or numeric.

- **MODEL**

- MODEL dependent = < fixed-effects >< / options >;
- The MODEL statement names a single dependent variable and the fixed effects, which determine the **X** matrix of the mixed model.

- **RANDOM**

- RANDOM random-effects < / options >;
- Define **Z**
- Define **γ**
- Define **G**

- **REPEATED**

- REPEATED < repeated-effect >< / options >;
- Specify the R matrix in the mixed model.

3. Dataset: Protein milk data set (in the class website)

Data description: Percentage protein content of milk samples at weekly intervals from each of 25 cows on barley diet, 27 cows on mixed diet and 27 cows on lupins diet.

4. STATA output of the analysis

- **Read data into STATA**

```
.log using c:\data\lab7sup, replace
. set mem 50m
(51200k)
. set matsize 800
. *read the data into STATA from three text files
. infile y1 y2 y3 y4 y5 y6 y7 y8 y9 y10 y11 y12 y13 y14 y15 y16 y17 y18 y19 using
c:\data\cows.barley.data, clear
(25 observations read)
. gen id=_n
. gen grp=1
. count
    25
. save c:\data\milk1, replace
file c:\data\milk1.dta saved
. infile y1 y2 y3 y4 y5 y6 y7 y8 y9 y10 y11 y12 y13 y14 y15 y16 y17 y18 y19 using
c:\data\cows.mixed.data, clear
```

```
(27 observations read)
. gen id=_n+25
. gen grp=2
. count
    27
. save c:\data\milk2, replace
file c:\data\milk2.dta saved
. infile y1 y2 y3 y4 y5 y6 y7 y8 y9 y10 y11 y12 y13 y14 y15 y16 y17 y18 y19 using
c:\data\cows.lupins.data, clear
(27 observations read)
. gen id=_n+52
. gen grp=3
. append using "c:\data\milk1.dta" , nolabel
. append using "c:\data\milk2.dta", nolabel
. sort id
. save c:\data\milk, replace
file c:\data\milk.dta saved
```

- **Reshape to long format**

```
. reshape long y, i(id) j(t)
(note: j = 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19)
```

| Data | wide | -> | long |
|------------------------|---------------|----|------|
| Number of obs. | 79 | -> | 1501 |
| Number of variables | 21 | -> | 4 |
| j variable (19 values) | | -> | t |
| xij variables: | y1 y2 ... y19 | -> | y |

```
. *recode missing value
. replace y=. if y==0
(164 real changes made, 164 to missing)

. label var y "Protein content"
. label var t "Weeks"
. label define group 1 "barley diet" 2 "mixed diet" 3 "lupins diet"
. label value grp group
. save c:\data\milk, replace
file c:\data\milk.dta saved
```

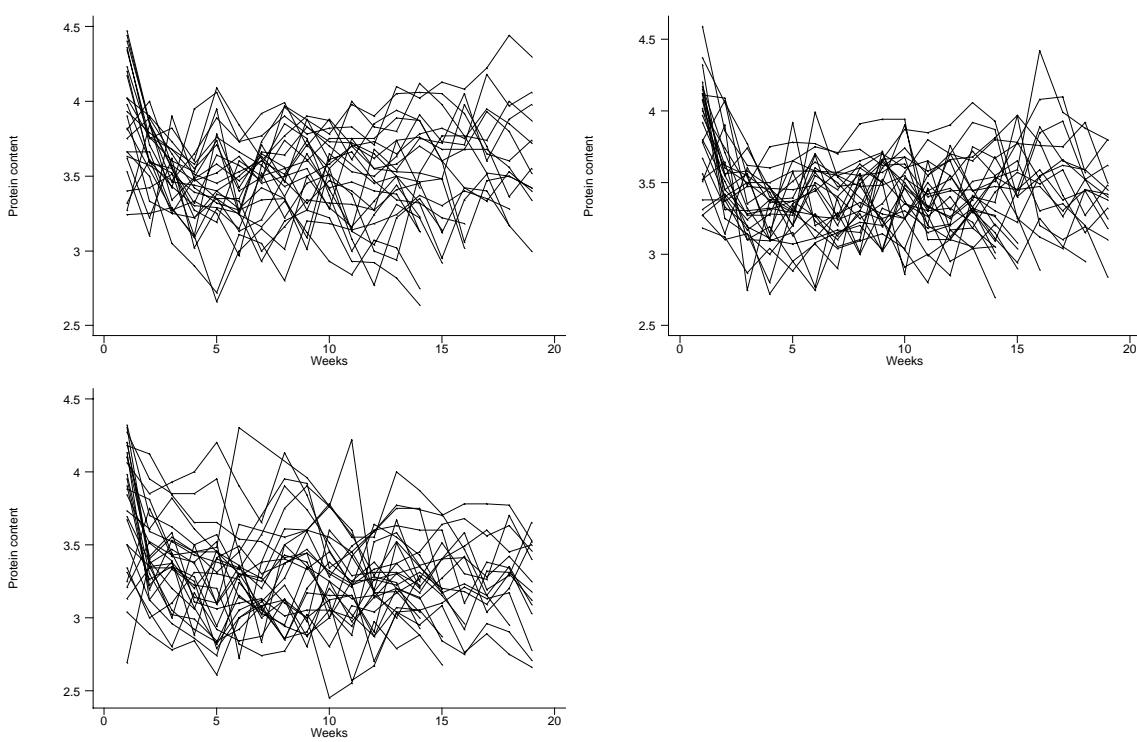
- **Some plots**

```
. *spaghetti plots
. sort id t grp
. graph y t if grp==1, c(L) s(.) xlab ylab saving(g1,replace)
. graph y t if grp==2, c(L) s(.) xlab ylab saving(g2,replace)
. graph y t if grp==3, c(L) s(.) xlab ylab saving(g3,replace)
. graph using g1 g2 g3
```

Milk Data Analysis

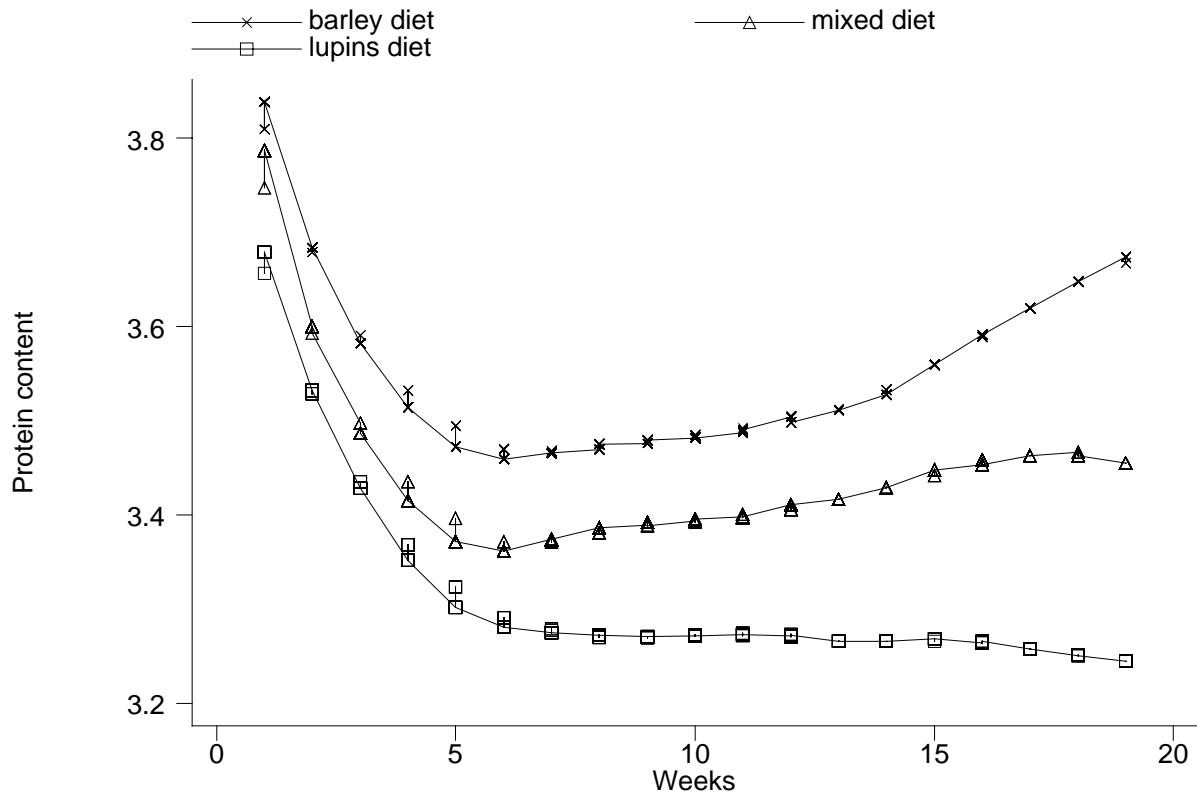
Analysis of Longitudinal Data

Biostatistics(140.655)



```
. *smoothing plots
. gen y1 = y if grp == 1
(1076 missing values generated)
. gen y2 = y if grp == 2
(1042 missing values generated)
. gen y3 = y if grp == 3
(1048 missing values generated)
. ksm y1 t, gen(sml) lowess bw(0.6) nograph
. ksm y2 t, gen(sm2) lowess bw(0.6) nograph
. ksm y3 t, gen(sm3) lowess bw(0.6) nograph
. label var sml "barley diet"
. label var sm2 "mixed diet"
. label var sm3 "lupins diet"

. sort t
. graph sml sm2 sm3 t, c(l11)s(x) xlab ylab l1("Protein content")
```



```
. drop sm1 sm2 sm3 y1 y2 y3
. save c:\data\milk1, replace
file c:\data\milk1.dta saved
```

- Set to longitudinal data

```
. tsset id t
    panel variable: id, 1 to 79
    time variable: t, 1 to 19

. *description of the longitudinal data
. xtdes

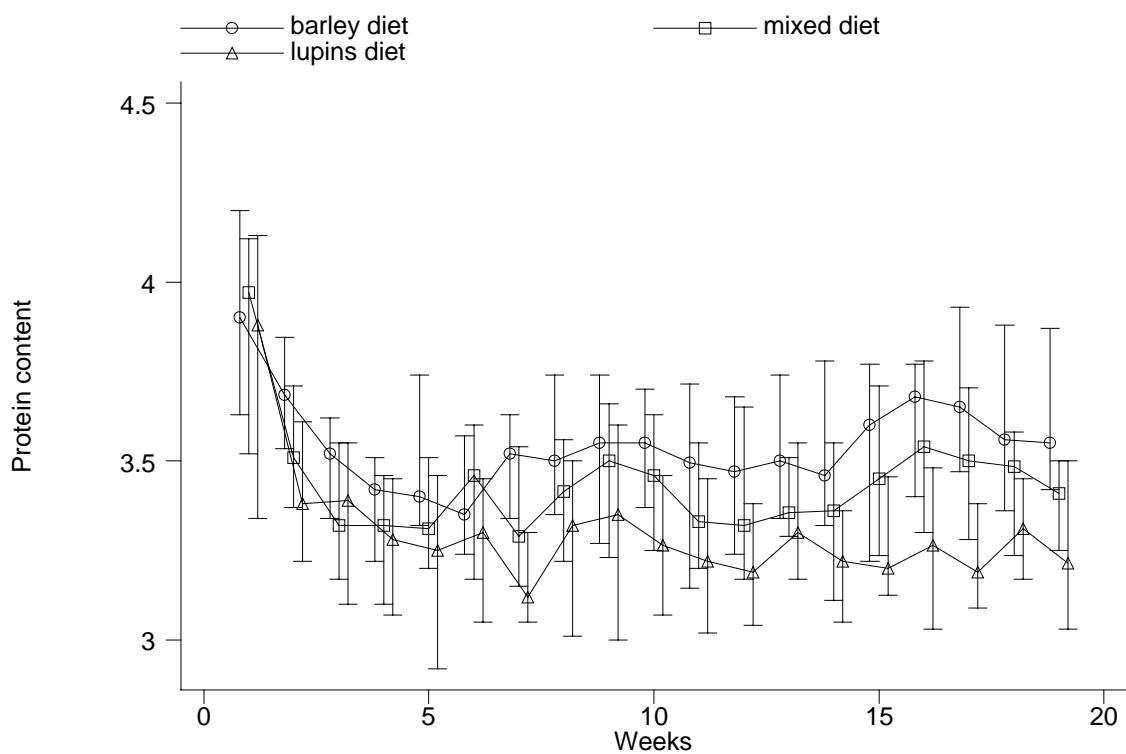
id: 1, 2, ..., 79                                n =      79
t: 1, 2, ..., 19                                T =      19
    Delta(t) = 1; (19-1)+1 = 19
    (id*t uniquely identifies each observation)
Distribution of T_i:   min      5%     25%     50%     75%     95%     max
                      19       19       19       19       19       19       19
Freq.  Percent     Cum. |  Pattern
-----+-----
79    100.00  100.00 |  11111111111111111111
-----+-----
79    100.00          |  XXXXXXXXXXXXXXXXXXXXXX
```

```
. xtgraph y, group(grp) av(median) bar(iqr) xlab ylab offset(.2)
```

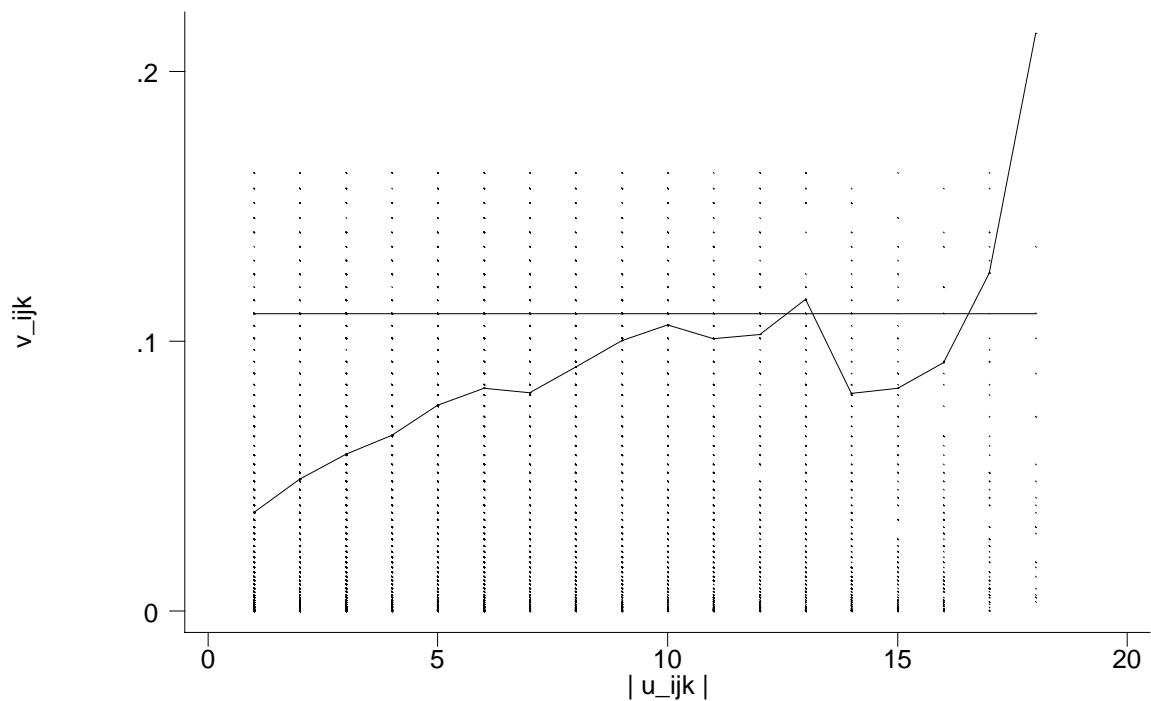
Milk Data Analysis

Analysis of Longitudinal Data

Biostatistics(140.655)



```
. variogram y, discrete
Computing ANOVA model for v in ulag
Variogram of y (13 percent of v_ijk's excluded)
```



```
* variogram indicates exponential correlation
```

• **Specify the mean model**

*create design matrix for mean model
. tab grp, gen(bg)

| grp | Freq. | Percent | Cum. |
|-------------|-------|---------|--------|
| barley diet | 475 | 31.65 | 31.65 |
| mixed diet | 513 | 34.18 | 65.82 |
| lupins diet | 513 | 34.18 | 100.00 |
| Total | 1501 | 100.00 | |

```
. gen b1=t

. replace b1=3 if t>3
(1264 real changes made)
. gen b2= (t-3)*(t>3)
. gen b3= (t-3)*(t-3)*(t>3)
. sort id t

. prais y bg1 bg2 bg3 b1 b2 b3, noconst
```

Number of gaps in sample: 88 (gap count includes panel changes)
(note: computations for rho restarted at each gap)

Iteration 0: rho = 0.0000
Iteration 1: rho = 0.6050
Iteration 2: rho = 0.6096
Iteration 3: rho = 0.6097
Iteration 4: rho = 0.6097
Iteration 5: rho = 0.6097

Prais-Winsten AR(1) regression -- iterated estimates

| Source | SS | df | MS | Number of obs | = | 1337 |
|----------|------------|------|------------|---------------|---|---------|
| Model | 2930.0779 | 6 | 488.346317 | F(6, 1331) | = | 8614.52 |
| Residual | 75.4527555 | 1331 | .056688772 | Prob > F | = | 0.0000 |
| Total | 3005.53066 | 1337 | 2.24796609 | R-squared | = | 0.9749 |

| y | Coef. | Std. Err. | t | P> t | [95% Conf. Interval] |
|-----|----------|-----------|--------|-------|----------------------|
| bg1 | 4.140753 | .0519486 | 79.71 | 0.000 | 4.038843 4.242664 |
| bg2 | 4.036527 | .0515201 | 78.35 | 0.000 | 3.935457 4.137596 |
| bg3 | 3.930836 | .0515166 | 76.30 | 0.000 | 3.829774 4.031899 |
| b1 | -.221672 | .0186047 | -11.91 | 0.000 | -.2581697 -.1851742 |
| b2 | .0030986 | .009073 | 0.34 | 0.733 | -.0147003 .0208975 |
| b3 | -.000164 | .0005728 | -0.29 | 0.775 | -.0012876 .0009596 |
| rho | .6096952 | | | | |

Durbin-Watson statistic (original) 0.700758
Durbin-Watson statistic (transformed) 2.058911

```
. xtgee y bg1 bg2 bg3 b1 b2 b3, noconst i(id) t(t) corr(ar1)
```

note: observations not equally spaced
modal spacing is delta t = 1
8 groups omitted from estimation

Iteration 1: tolerance = .00520863

Iteration 2: tolerance = .00020207
 Iteration 3: tolerance = 8.292e-06
 Iteration 4: tolerance = 3.451e-07

GEE population-averaged model
 Group and time vars: id t Number of obs = 1211
 Link: identity Number of groups = 71
 Family: Gaussian Obs per group: min = 14
 Correlation: AR(1) avg = 17.1
 Scale parameter: .0897981 max = 19
 Wald chi2(5) = 31728.78
 Prob > chi2 = 0.0000

| y | Coef. | Std. Err. | z | P> z | [95% Conf. Interval] |
|----------------|----------|-----------|-------|-----------|----------------------|
| bg1 4.132398 | .0550036 | 75.13 | 0.000 | 4.024593 | 4.240203 |
| bg2 4.051468 | .0541372 | 74.84 | 0.000 | 3.945361 | 4.157575 |
| bg3 3.912359 | .0543971 | 71.92 | 0.000 | 3.805743 | 4.018975 |
| b1 -.2222159 | .0197475 | -11.25 | 0.000 | -.2609202 | -.1835115 |
| b2 -.0030645 | .0095473 | -0.32 | 0.748 | -.0217768 | .0156478 |
| b3 .0002933 | .0006033 | 0.49 | 0.627 | -.0008892 | .0014757 |

```
. *create a text file for SAS
. outfile id t y grp bg1 bg2 bg3 b1 b2 b3 using c:\data\milk.txt,nolabel replace
. log close
```

5. Refit the model using SAS

```
LIBNAME lab 'c:\data';

DATA milk;
INFILE 'c:\data\milk.txt';
INPUT id t y grp bg1 bg2 bg3 b1 b2 b3;
RUN;

*ML ESTIMATE WITH AR1 CORRELATION STRUCTURE*;
PROC MIXED DATA=milk METHOD = ML;
CLASS id;
MODEL y = bg1 bg2 bg3 b1 b2 b3/ NOINT SOLUTION CL;
REPEATED /SUBJECT=ID TYPE = AR(1);
RUN;
```

Covariance Parameter Estimates

| Cov Parm | Subject | Estimate |
|----------|----------|----------|
| AR(1) | id | 0.6415 |
| | Residual | 0.09503 |

Fit Statistics

| | |
|--------------------------|-------|
| -2 Log Likelihood | -16.0 |
| AIC (smaller is better) | -0.0 |
| AICC (smaller is better) | 0.1 |
| BIC (smaller is better) | 18.9 |

Solution for Fixed Effects

| Effect | Estimate | Standard Error | DF | t Value | Pr > t | Alpha | Lower | Upper |
|--------|----------|----------------|------|---------|---------|-------|----------|----------|
| bg1 | 4.1414 | 0.05317 | 76 | 77.89 | <.0001 | 0.05 | 4.0355 | 4.2473 |
| bg2 | 4.0406 | 0.05259 | 76 | 76.83 | <.0001 | 0.05 | 3.9358 | 4.1453 |
| bg3 | 3.9287 | 0.05261 | 76 | 74.68 | <.0001 | 0.05 | 3.8240 | 4.0335 |
| b1 | -0.2216 | 0.01853 | 1255 | -11.96 | <.0001 | 0.05 | -0.2579 | -0.1852 |
| b2 | 0.001592 | 0.009366 | 1255 | 0.17 | 0.8651 | 0.05 | -0.01678 | 0.01997 |
| b3 | -0.00010 | 0.000591 | 1255 | -0.17 | 0.8647 | 0.05 | -0.00126 | 0.001059 |

Type 3 Tests of Fixed Effects

| Effect | Num DF | Den DF | F Value | Pr > F |
|--------|--------|--------|---------|--------|
| | | | | |
| bg1 | 1 | 76 | 6066.31 | <.0001 |
| bg2 | 1 | 76 | 5903.19 | <.0001 |
| bg3 | 1 | 76 | 5577.56 | <.0001 |
| b1 | 1 | 1255 | 143.02 | <.0001 |
| b2 | 1 | 1255 | 0.03 | 0.8651 |
| b3 | 1 | 1255 | 0.03 | 0.8647 |

```
*REML ESTIMATE WITH AR1 CORRELATION STRUCTURE*;
PROC MIXED DATA=milk METHOD = REML;
CLASS id;
MODEL y = bg1 bg2 bg3 b1 b2 b3/ NOINT SOLUTION CL;
REPEATED /SUBJECT=ID TYPE = AR(1);
RUN;
```

Covariance Parameter Estimates

| Cov Parm | Subject | Estimate |
|----------|----------|----------|
| AR(1) | id | 0.6465 |
| | Residual | 0.09645 |

Fit Statistics

| | |
|--------------------------|------|
| -2 Res Log Likelihood | 28.9 |
| AIC (smaller is better) | 32.9 |
| AICC (smaller is better) | 32.9 |
| BIC (smaller is better) | 37.6 |

Solution for Fixed Effects

| Effect | Estimate | Standard Error | DF | t Value | Pr > t | Alpha | Lower | Upper |
|--------|----------|----------------|------|---------|---------|-------|----------|----------|
| bg1 | 4.1413 | 0.05353 | 76 | 77.36 | <.0001 | 0.05 | 4.0347 | 4.2479 |
| bg2 | 4.0405 | 0.05294 | 76 | 76.33 | <.0001 | 0.05 | 3.9351 | 4.1460 |
| bg3 | 3.9287 | 0.05295 | 76 | 74.19 | <.0001 | 0.05 | 3.8233 | 4.0342 |
| b1 | -0.2215 | 0.01858 | 1255 | -11.92 | <.0001 | 0.05 | -0.2579 | -0.1850 |
| b2 | 0.001579 | 0.009438 | 1255 | 0.17 | 0.8672 | 0.05 | -0.01694 | 0.02010 |
| b3 | -0.00011 | 0.000595 | 1255 | -0.18 | 0.8579 | 0.05 | -0.00127 | 0.001061 |

Milk Data Analysis

Analysis of Longitudinal Data Biostatistics(140.655)

Type 3 Tests of Fixed Effects

| Effect | Num DF | Den DF | F Value | Pr > F |
|--------|--------|--------|---------|--------|
| bg1 | 1 | 76 | 5984.63 | <.0001 |
| bg2 | 1 | 76 | 5825.74 | <.0001 |
| bg3 | 1 | 76 | 5504.42 | <.0001 |
| b1 | 1 | 1255 | 142.13 | <.0001 |
| b2 | 1 | 1255 | 0.03 | 0.8672 |
| b3 | 1 | 1255 | 0.03 | 0.8579 |

```
*ML ESTIMATE WITH EXPONENTIAL CORRELATION STRUCTURE* ;
PROC MIXED DATA=milk METHOD = ML;
CLASS id;
MODEL y = bg1 bg2 bg3 b1 b2 b3/ NOINT SOLUTION CL;
REPEATED /SUBJECT=ID TYPE = SP(POW) (t);
RUN;
```

Covariance Parameter Estimates

| Cov Parm | Subject | Estimate |
|----------|---------|----------|
| SP(POW) | id | 0.6415 |
| Residual | | 0.09503 |

Fit Statistics

| | |
|--------------------------|-------|
| -2 Log Likelihood | -16.0 |
| AIC (smaller is better) | -0.0 |
| AICC (smaller is better) | 0.1 |
| BIC (smaller is better) | 18.9 |

Solution for Fixed Effects

| Effect | Estimate | Error | DF | t Value | Pr > t | Alpha | Lower | Upper |
|--------|----------|----------|------|---------|---------|-------|----------|----------|
| bg1 | 4.1414 | 0.05317 | 76 | 77.89 | <.0001 | 0.05 | 4.0355 | 4.2473 |
| bg2 | 4.0406 | 0.05259 | 76 | 76.83 | <.0001 | 0.05 | 3.9358 | 4.1453 |
| bg3 | 3.9287 | 0.05261 | 76 | 74.68 | <.0001 | 0.05 | 3.8240 | 4.0335 |
| b1 | -0.2216 | 0.01853 | 1255 | -11.96 | <.0001 | 0.05 | -0.2579 | -0.1852 |
| b2 | 0.001592 | 0.009366 | 1255 | 0.17 | 0.8651 | 0.05 | -0.01678 | 0.01997 |
| b3 | -0.00010 | 0.000591 | 1255 | -0.17 | 0.8647 | 0.05 | -0.00126 | 0.001059 |

Type 3 Tests of Fixed Effects

| Effect | Num DF | Den DF | F Value | Pr > F |
|--------|--------|--------|---------|--------|
| bg1 | 1 | 76 | 6066.31 | <.0001 |
| bg2 | 1 | 76 | 5903.19 | <.0001 |
| bg3 | 1 | 76 | 5577.56 | <.0001 |
| b1 | 1 | 1255 | 143.02 | <.0001 |
| b2 | 1 | 1255 | 0.03 | 0.8651 |
| b3 | 1 | 1255 | 0.03 | 0.8647 |