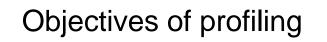
Lecture 8 Applications of Multilevel Models to Profiling of Health Care Providers

### Outline

- What is profiling?
  - Definitions
  - Statistical challenges
  - Centrality of multi-level analysis
- Fitting Multilevel Models with Winbugs:
  - A toy example on institutional ranking
- · Profiling medical care providers: a case-study
  - Hierarchical logistic regression model
  - Performance measures
  - Comparison with standard approaches

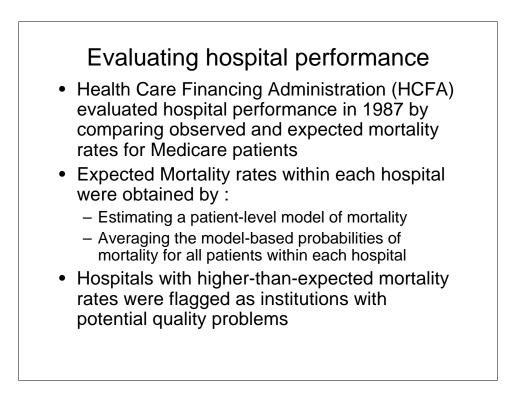
# What is profiling?

- Profiling is the process of comparing quality of care, use of services, and cost with normative or community standards
- Profiling analysis is developing and implementing performance indices to evaluate physicians, hospitals, and care-providing networks



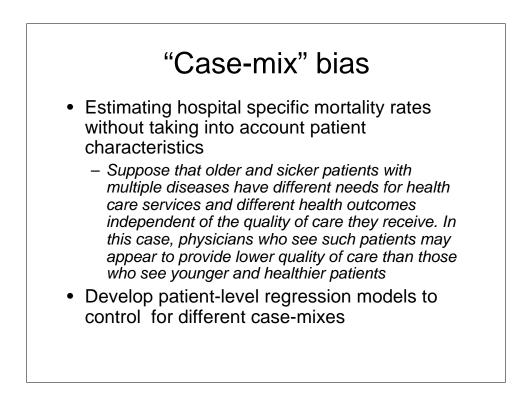
- Estimate provider-specific performance measures:
  - measures of utilization
  - patients outcomes
  - satisfaction of care
- Compare these estimates to a community or a normative standard





# **Statistical Challenges**

- Hospital profiling needs to take into account
  - Patients characteristics
  - Hospital characteristics
  - Correlation between outcomes of patients within the same hospital
  - Number of patients in the hospital
- These data characteristics motivate the centrality of multi-level data analysis



### Within cluster correlation

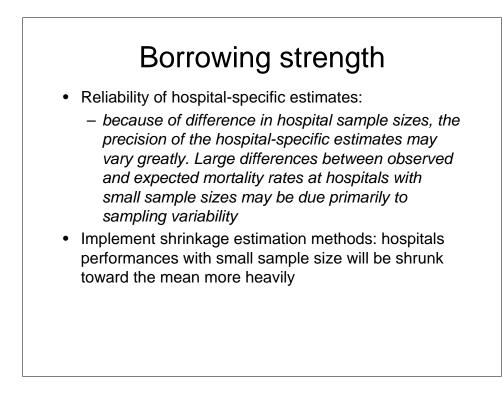
- Hospital practices may induce a strong correlation among patient outcomes within hospitals even after accounting for patients characteristics
- Extend standard regression models to multi-level models that take into account the clustered nature of the data

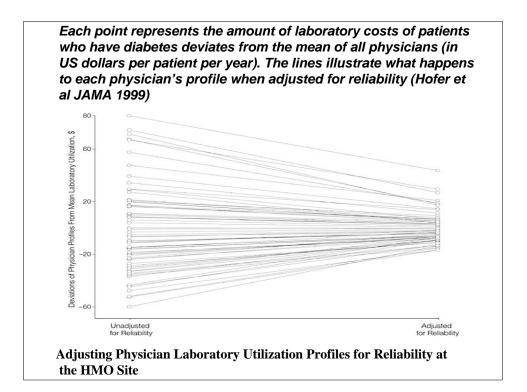
# Health care quality data are multi-level!

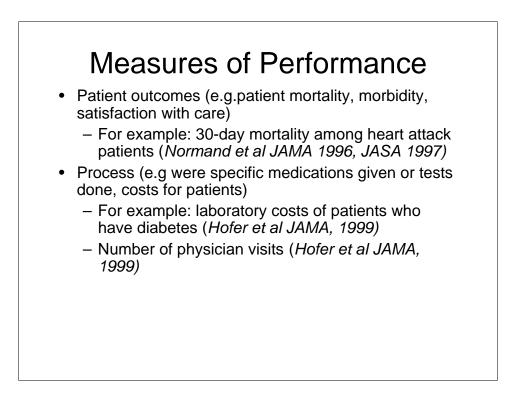
- · Data are clustered at multiple-levels
  - Patients clustered by providers, physicians, hospitals, HMOs
  - Providers clustered by health care systems, market areas, geographic areas
- Provider sizes may vary substantially
- Covariates at different levels of aggregation: patient-level, provider level
- Statistical uncertainty of performance estimates need to take into account:
  - Systematic and random variation
  - Provider-specific measures of utilization, costs

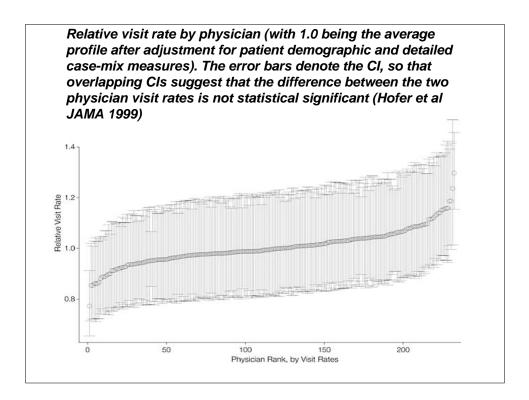
# Sampling variability versus systematic variability

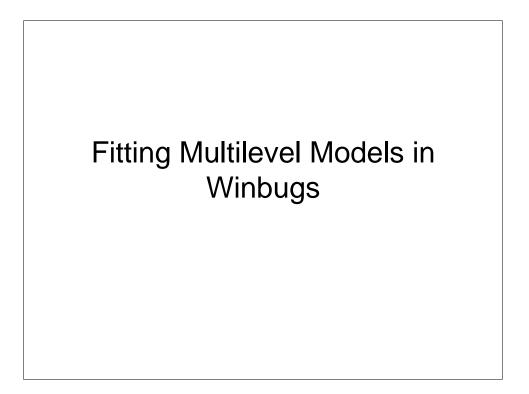
- "Sampling variability": statistical uncertainty of the hospital-specific performance measures
- "Systematic variability" : variability between hospitals performances that can be possibly explained by hospital-specific characteristics (aka "natural variability")
- Develop multi-level models that incorporate both patient-level and hospital-level characteristics

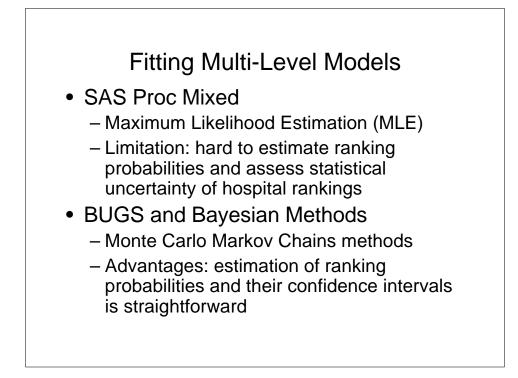


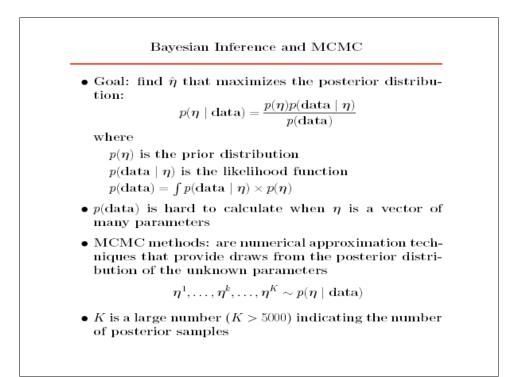


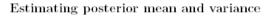












- $\hat{\eta} = E[\eta \mid \text{data}]$  easy to calculate by taking the average of the sampled values.
- $SE(\hat{\eta}) = \sqrt{V[\eta \mid data]}$  easy to calculate by taking the variance of the sampled values
- In our case, WINBUGS will produce posterior samples of all parameters of interests.
- For example, let  $\beta_{0i}^k$  be the k th sample from  $p(\beta_{0i} \mid \text{data})$ , where  $\beta_{0i}$  is the hospital-specific log-odds ratio of death
- The posterior probability that  $\beta_{01}$  is larger than  $\beta_{02}$  (that is, hospital 1 is worse than hospital 2), can be easily estimated by counting how many times the posterior samples of  $\beta_{01}$  are larger than the posterior samples of  $\beta_{02}$

$$\widehat{P}(\beta_{01} > \beta_{02} \mid \textbf{data}) = \frac{1}{K} \sum_{k=1}^{K} I(\beta_{01}^k > \beta_{02}^k)$$

# Toy example on using WinBUGS for hospital performance ranking

This example considers mortality rates in 12 hospitals performing cardiac surgery in babies. The data are shown below.

A	47	0
	148	18
B C D E F G	119	8
D	810	46
E	211	8
F	196	13
G	148	9
Н	215	31
I	207	14
J	97	8
K	256	29
L	360	24

#### A Multi-level model for hospital ranking

- Let r<sub>i</sub> the number of deaths for hospital i
- let n<sub>i</sub> the number of surgeries performed in hospital i

We assume

 $\begin{array}{ll} \tau_i & \sim \ \mathrm{Bin}(p_l,n_l) \\ \mathrm{logit} p_l &= \ \mu + b_l \\ b_l & \sim \ N(0,\sigma^2) \end{array}$ 

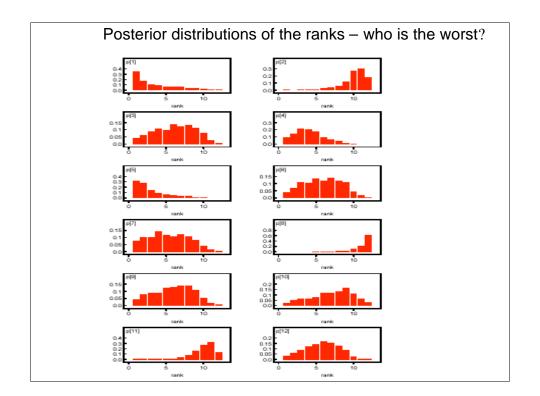
where

- p<sub>i</sub> is the hospital-specific probability of death
- *p* = exp(μ)/(1 + exp(μ))
   is the probability of death for
   b<sub>i</sub> = 0

Goal: identify the "aberrant" hospitals

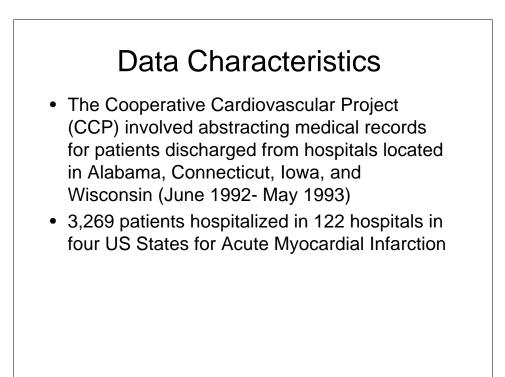
```
model
{
    for( i in 1 : N ) {
        b[i] ~ dnorm(mu,tau)
        r[i] ~ dbin(p[i],n[i])
        logit(p[i]) <- b[i]
        }
        pop.mean <- exp(mu) / (1 + exp(mu))
        mu ~ dnorm(0.0,1.0E-6)
        sigma <- 1 / sqrt(tau)
        tau ~ dgamma(0.001,0.001)
}</pre>
```

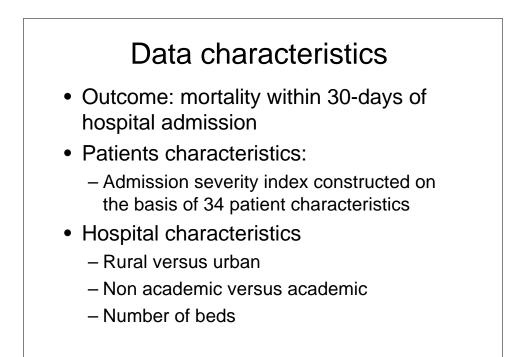
mean	
mean	
mean	
	sd
0.05357	0.01959
0.1026	0.02203
0.07102	0.01701
0.05947	0.008078
0.05252	0.01354
0.06867	0.01401
0.06796	0.01597
0.1217	0.02196
0.06943	0.01435
0.07859	0.0193
0.1019	0.01745
0.06893	0.01185
0.07246	0.0105
	0.05357 0.1026 0.07102 0.05947 0.05252 0.06867 0.06796 0.1217 0.06943 0.07859 0.1019 0.06893



Hospital Profiling of Mortality Rates for Acute Myocardial Infarction Patients (Normand et al JAMA 1996, JASA 1997)

- Data characteristics
- Scientific goals
- Multi-level logistic regression model
- Definition of performance measures
- Estimation
- Results
- Discussion





# Admission severity index (Normand et al 1997 JASA)

Χ <sub>ρ</sub>	$\hat{\beta}_{p}$	Xp	$\hat{\beta}_{p}$
Constant	5.5726	LV function proxies:	
Socio-demographic:		Cardiac arrest	.9069
(Age65)	.0681	Gallop rhythm	0310
(Age-65) <sup>2</sup>	0010	Cardiomegaly	0094
Admission history:		Hx CHF	1061
Hx cancer	1740	Rales and pulmonary edema	.1520
Admission severity:		Laboratory results:	
Mobility status		Albumin $> 3$ (g/dl)	4828
Walked independently	2740	Albumin missing	4793
Unable to walk	.4700	Log <sub>10</sub> [BUN (mg/dl)]	1.0613
Mobility missing	.3669	BUN missing	1.4583
Body mass index (kg/m <sup>2</sup> )	0259	Creatinine > 2 (mg/dl)	.3279
Body mass missing	1525	Creatinine missing	.1937
Respiration rate breaths/min		Diagnostic test results:	
Respiration (if $\geq$ 12)	.0429	Conduction disturbance	.4084
Respiration < 12	3.4840	No EKG (vs EKG reading)	.5050
Respiration missing	2.2666	No MI on EKG (vs MI on EKG)	1430
Ventricular rate > 100	.1564	Anterior MI (vs other MI)	.4384
Log <sub>10</sub> (MAP)	-4.7101	Lateral MI (vs other MI)	.2908
MAP missing	-10.1796	Posterior MI (vs other MI)	.6416
Shock	1.6194	Lateral and posterior MI	8767

# Scientific Goals: Identify "aberrant" hospitals in terms of several performance measures Report the statistical uncertainty associated with the ranking of the

"worst hospitals"
Investigate if hospital characteristics explain heterogeneity of hospitalspecific mortality rates

# Hierarchical logistic regression model

- I: patient level, within-provider model
- Patient-level logistic regression model with random intercept and random slope
- II: between-providers model
  - Hospital-specific random effects are regressed on hospital-specific characteristics

#### Patient-level model

- $Y_{ij}$  is the binary indicator of death within 30 days of admission for patient j at hospital i
- severity  $_{ij}$  is the severity index for patient j at hospital i
- severity is average severity index

 $\mathbf{logit} P(Y_{ij} = 1) = \beta_{0i} + \beta_{1i}(\mathbf{severity}_{ij} - \overline{\mathbf{severity}})$ 

- $\beta_{0i}$  and  $\beta_{1i}$  are random intercept and slope
- $\beta_{0i}$  denotes the log-odds ratio of death for hospital *i* having patients with severity equal to the average
- $\beta_{1i}$  denotes the hospital-specific association between severity and logit of probability of death

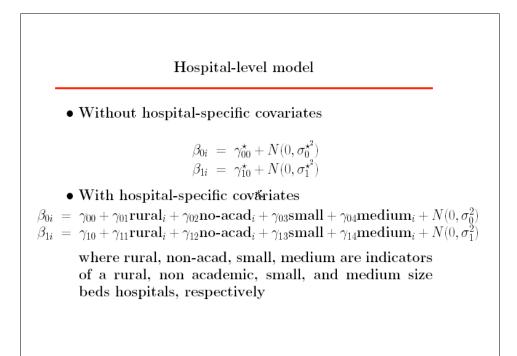


Table 1. Patient and Hospital Characteristics in the Study Cohort								
	25th percentile	Median	Mean	75th percentile				
Observed Mortality								
Across hospitals	.14	.22	.22	.29				
Admission severity								
Across patients	-2.47	-1.80	-1.65	99				
Across hospitals	-1.47	-1.49	-1.47	-1.22				
Hospital characteristics		% of patients	4	% of Hospitals				
Rural (vs. urban)		54		76				
Nonacademic (vs. academic)		79		88				
Number of beds	,							
<100 (small)		29	64					
101-299 (medium)		27	21					
≥300 (large)	,	44	15					

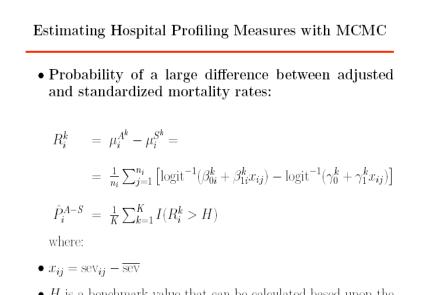
### Hospital-Performance Measures • Let $\mu_i^A$ be the "adjusted" mortality rate for hospital *i* • Let $\mu_i^S$ be the "standardized" mortality rate for a "reference" hospital • We assume that a provider's performance is poor if the probability that $\mu_i^A - \mu_i^S$ being bigger than some benchmark value is large. We estimate: $P_i^{A-S} = P(\mu_i^A - \mu_i^S > \text{benchmark}),$ where $\mu_i^A = \frac{1}{n_i} \sum_{j=1}^{n_i} P(Y_{ij} = 1 \mid \beta_{0i}, \beta_{1i}, \text{sev})$ $= \frac{1}{n_i} \sum_{j=1}^{n_i} \log t^{-1}(\beta_{0i} + \beta_{1i}(\text{sev}_{ij} - \overline{\text{sev}}))$ $\mu_i^S = \frac{1}{n_i} \sum_{j=1}^{n_i} P(Y_{ij} = 1 \mid \gamma_0, \gamma_1, \text{sev})$ $= \frac{1}{n_i} \sum_{j=1}^{n_i} \log t^{-1}(\gamma_0 + \gamma_1(\text{sev}_{ij} - \overline{\text{sev}}))$

#### Hospital-Performance Measures

- Let  $Y_i^{\star} = E[Y_i \mid, \overline{sev}, \beta]$  be the probability of death for an "average" patient with severity index equal to  $\overline{sev}$ treated in hospital *i*
- Let *M* be the median probability of death for the same "average" patient across all hospitals
- We define a hospital performance measure as the probability of excess mortality for the average patient
- The performance of hospital i is poor if the probability of death for an "average" patient treated in hospital i is large compared to M. More specifically, we are interested to estimate:

$$P_i^\star = P(Y_i^\star > M)$$

$$= P(logit^{-1}(\beta_{0i}) > M)$$



 $\bullet~H$  is a benchmark value that can be calculated based upon the distribution of  $R^k_i$  across hospitals

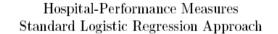
#### Estimating Hospital Profiling Measures with MCMC

• Probability of excess mortality for the average patient:

$$\hat{P}_{i}^{\star} = \frac{1}{K} \sum_{k=1}^{K} I(\text{logit}^{-1}(\beta_{0i}^{k}) > M)$$

where:

• *M* is the median of  $\{ \text{logit}^{-1}(\beta_{0i}^k), i = 1, \dots, 96 \}$ 



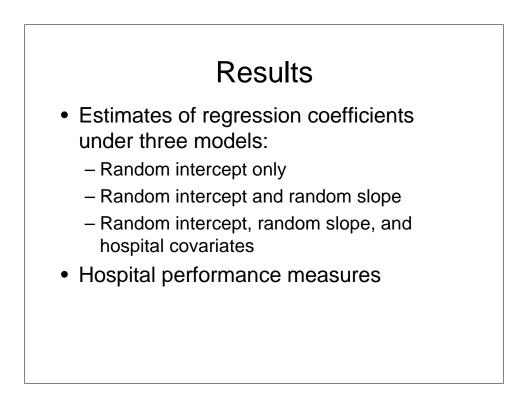
- The HCFA's algorithm to identify "aberrant hospitals" does not rely on multilevel models
- A logistic regression is fitted to the data, and zscores were derived from the standardized difference between observed and expected mortality in each hospital. More specifically

$$\begin{aligned} z_i &= n_i (\bar{Y}_i - \bar{p}_i) / \sqrt{\sum_{j=1}^{n_i} \hat{p}_{ij} (1 - \hat{p}_{ij})} \\ \text{where} \\ \hat{p}_{ij} &= \text{logit}^{-1} (\hat{\beta}_{0i} + \hat{\beta}_{1i} (\text{sev}_{ij} - \overline{\text{sev}})) \end{aligned}$$

• hospitals with  $z_i \ge 1.645$  (top 5%) were classified as "aberrant"

### Comparing measures of hospital performance

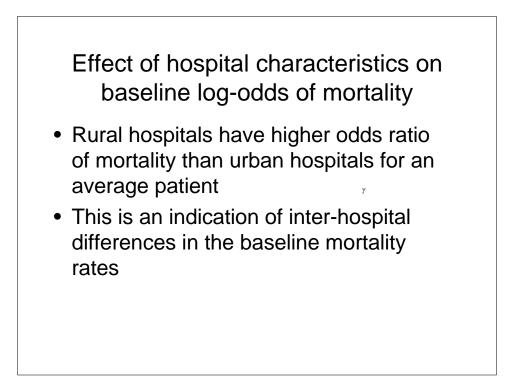
- Three measures of hospital performance
  - Probability of a large difference between adjusted and standardized mortality rates
  - Probability of excess mortality for the average patient
  - Z-score

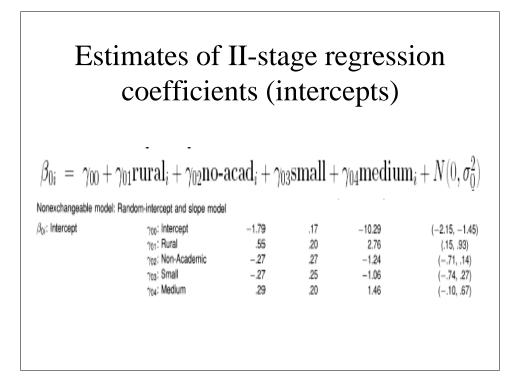


	Tab	le 2. Regression Es	timates					
Level I	Level II	Estimated posterior summaries						
parameter	parameter	Mean	SD	Mean/SD	Percentiles (2.5, 97.			
Exchangeable model: Rando	m-intercept model							
β <sub>0i</sub> : Intercept	$\gamma$ : Intercept $\sigma_{\mathcal{B}_{n}}^{2}$ : Variance	-1.70 (.31) <sup>2</sup>	.07 .05	-24.29	(-1.85, -1.57) (.01, .22)			
β <sub>1</sub> : Severity – severity	20	1.03	.05	20.60	(.93, 1.13)			
Exchangeable model: Rando	m-intercept and slope model							
β <sub>0i</sub> : Intercept	γ <sub>00</sub> : Intercept	-1.72	.08	-21.53	(-1.87, -1.56)			
β <sub>1/</sub> : Severity - severity	γ <sub>10</sub> : Intercept	1.03	.05	19.67	(.94, 1.15)			
			Estii	mated posterior mear	n			
	D: Variance			$\begin{pmatrix} (.42)^2 &03 \\03 & (.21)^2 \end{pmatrix}$	-			
Nonexchangeable model: Ra	ndom-intercept and slope mode	I		( (, / /				
β <sub>0/</sub> : Intercept	γ <sub>00</sub> : Intercept	-1.79	.17	-10.29	(-2.15, -1.45)			
	γ <sub>01</sub> : Rural	.55	.20	2.76	(.15, .93)			
	γ <sub>02</sub> : Non-Academic	27	.27	-1.24	(71, .14)			
	γ <sub>03</sub> : Small	27	.25	-1.06	(74, .27)			
	γ <sub>04</sub> : Medium	.29	.20	1.46	(10, .67)			
β <sub>1/</sub> : Severity – severity	γ <sub>10</sub> : Intercept	1.22	.13	9.18	(.96, 1.52)			
	γ11: Rural	.05	.16	.33	(27, .36)			
	γ <sub>12</sub> : Nonacademic	11	.17	64	(44, .23)			
	γ <sub>13</sub> : Small	08	.20	39	(50, .28)			
	γ <sub>14</sub> : Medium	29	.15	-1.88	(58, .01)			
			Esti	mated posterior mea	n			
	D: Variance			$\begin{pmatrix} (.35)^2 &03 \\03 & (.22)^2 \end{pmatrix}$				

# Estimates of log-odds of 30-day mortality for a ``average patient''

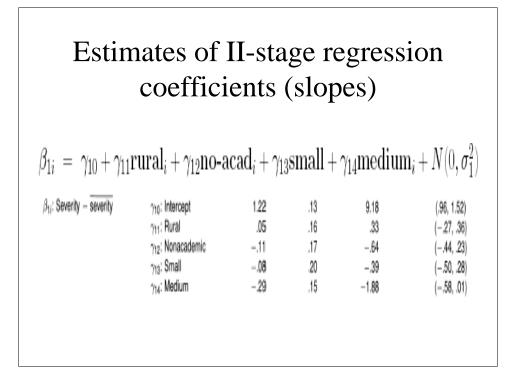
- Exchangeable model (without hospital covariates), random intercept and random slope:
  - We found that the 2.5 and 97.5 percentiles of the log-odds of 30-day mortality <u>for a patient with average admission</u> <u>severity</u> is equal to (-1.87,-1.56), corresponding to (0.13,0.17) in the probability scale
- Non-Exchangeable model (with hospital covariates), random intercept and random slope:
  - We found that the 2.5 and 97.5 percentiles for the log-odds of 30-day mortality <u>for a patient with average admission</u> <u>severity treated in a large, urban, and academic</u> <u>hospital is equal to (-2.15,-1.45)</u>, corresponding to (0.10,0.19) in probability scale



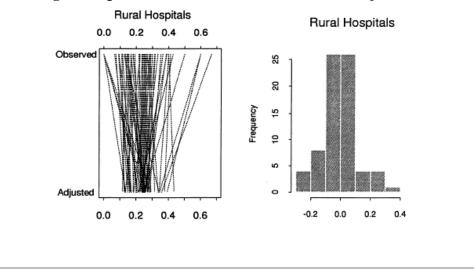


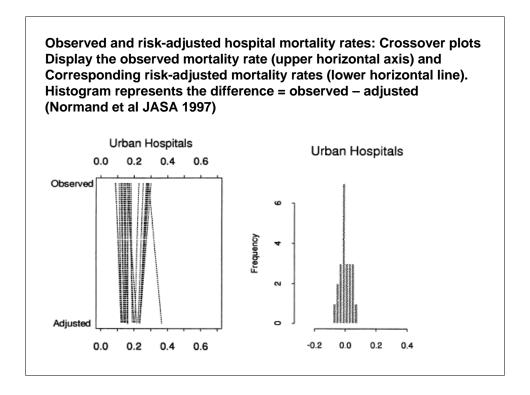
Effects of hospital characteristics on associations between severity and mortality (slopes)

- The association between severity and mortality is ``modified'' by the size of the hospitals
- Medium-sized hospitals having smaller severity-mortality associations than large hospitals
- This indicates that the effect of clinical burden (patient severity) on mortality differs across hospitals



Observed and risk-adjusted hospital mortality rates: Crossover plo Display the observed mortality rate (upper horizontal axis) and Corresponding risk-adjusted mortality rates (lower horizontal line) Histogram represents the difference = observed - adjusted





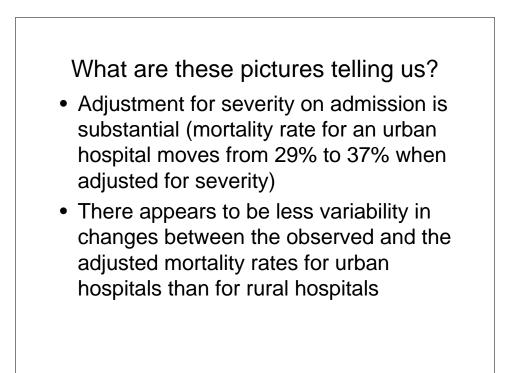
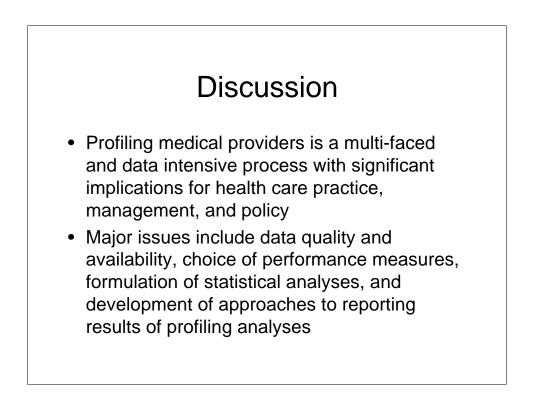


	Table 4. HCFA Highest and Lowest Ranked Hospitals												
					Random	intercept	Rando	m interc	ept and s	lope			
	No. of AMI	No.	Hospital	Academic	Hospital	HC	FA	₽́ <sup>A</sup>	-S	Ŷ	A-S	-	Ŷ;
Hospital		(Y/N) size		zį	Rank	(%)	Rank	(%)	Rank	(%)	Ran		
1	54	19	R	N	М	3.83	1	36	1	25	1	89	1
28	6	4	R	N	М	2.55	2	10	7	15	3	70	3
2	18	7	R	N	S	2.55	3	12	5	19	2	32	9
10	62	18	R	Ν	М	2.51	4	16	2	7	19	71	2
90	8	4	R	N	S	2.00	5	15	3	13	5.5	13	28
43	27	6	R	Ν	S	1.95	6	3	43	11	8	22	17
15	81	22	U	Y	L	1.82	7	9	11	5	26	10	31
44	7	3	R	N	S	1.75	8	6	20	5	33	11	30
95	22	8	R	Ν	S	1.68	9	12	6	14	4	16	21
29	31	5	U	Ν	S	-1.75	93	0	84.5	1	74	0	94
39	6	0	R	N	S	-1.77	94	2	54	3	48.5	2	77
19	46	4	U	N	L	-1.80	95	0	90.5	0	90.5	0	94
42	70	11	U	Y	L	-2.01	96	0	94.0	0	94.5	0	94

NOTE: HCFA highest-ranked (z, > 1.55) and lowest-ranked (z, < -1.65) hospitals. The rank of each measure is from worst (1) to best (96). L denotes hospitals with  $\geq$ 300 beds, M denotes hospitals with 101-299 beds, S denotes hospitals with fewer than 101 beds. R denotes rural hospitals, and U denotes urban hospitals.

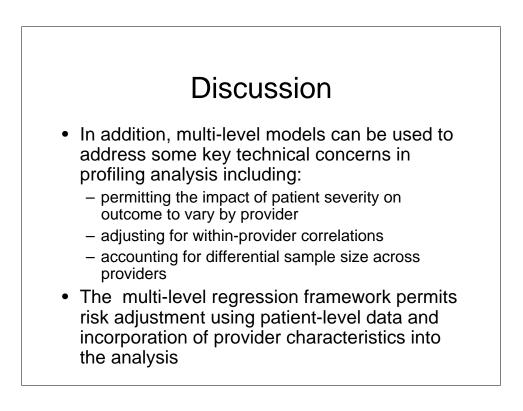
# Ranking of hospitals

- There was moderate disagreement among the criteria for classifying hospitals as ``aberrant"
- Despite this, hospital 1 is ranked as the worst. This hospital is rural, medium sized non-academic with an observed mortality rate of 35%, and adjusted rate of 28%



### Discussion

- Performance measures were estimated using a unifying statistical approach based on multi-level models
- Multi-level models:
  - take into account the hierarchical structure usually present in data for profiling analyses
  - Provide a flexible framework for analyzing a variety of different types of response variables and for incorporating covariates at different levels of hierarchal structure



# Discussion

- The consideration of provider characteristics as possible covariates in the second level of the hierarchical model is dictated by the need to explain as large a fraction as possible of the variability in the observed data
- In this case, more accurate estimates of hospital-specific adjusted outcomes will be obtained with the inclusion of hospital specific characteristics into the model

